Monopoly without a Monopolist: Economics of the Bitcoin Payment System

Gur Huberman, Jacob D. Leshno, Ciamac Moallemi Columbia Business School

Cryptocurrencies

Electronic payment systems

- Bitcoin being the first
- More than 10 systems have total balances of over \$1B
- New systems developed, offering new functionality

Decentralized, two-sided markets

- Users receive similar services to PayPal, Fedwire; Miners provide infrastructure
- Market design enabled by blockchain protocol

Novel economic structure

- Owned by no one
- Rules fixed by a computer protocol
- All (small) agents are price-takers

Cryptocurrencies

868 Currencies / 236 Assets / 5474 Markets Market Cap: \$159,7

Market Cap: \$159,773,994,232 / 24h Vol: \$6,528,166,064 / BTC Dominance: 47.1%

CryptoCurrency Market Capitalizations

Market Cap - Trade Volume - Trending - Tools - Search Currencies								
All	•	Currencies -	Assets -	USD 🗸				Next 100 \rightarrow View All
^ #	Na	ame	Market Cap	Price	Circulating Supply	Volume (24h)	% Change (24h)	Price Graph (7d)
1	B	Bitcoin	\$75,219,057,588	\$4545.48	16,548,100 BTC	\$2,281,740,000	6.46%	
2	\$	Ethereum	\$30,734,261,898	\$325.36	94,463,195 ETH	\$1,197,820,000	8.02%	~~~~~
3	B	Bitcoin Cash	\$10,615,945,842	\$640.94	16,563,063 BCH	\$586,182,000	21.33%	- my
4	•{	Ripple	\$8,465,783,474	\$0.220786	38,343,841,883 XRP *	\$174,811,000	4.79%	-my
5	G	Litecoin	\$3,984,112,940	\$75.45	52,807,757 LTC	\$787,911,000	10.99%	May
6	Ś	NEM	\$2,693,916,000	\$0.299324	8,999,999,999 XEM *	\$5,256,710	7.32%	-
7	Ð	Dash	\$2,518,908,128	\$334.01	7,541,348 DASH	\$38,438,700	6.03%	
8		ΙΟΤΑ	\$1,873,734,175	\$0.674119	2,779,530,283 MIOTA *	\$31,955,200	13.86%	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Source: https://coinmarketcap.com/ (accessed 9/6/2017)

Traditional Electronic Payment Systems

- Allows users to hold balances and make transfers
- Controlling authority
 - Provide trust, maintain infrastructure, sets usage fees
- Natural monopoly
 - Network externalities, fixed costs
 - Often requires regulation

Examples: Fedwire, Venmo, PayPal, SWIFT, M-Pesa

Traditional Payment Systems vs. Bitcoin



Traditional Payment Systems vs. Bitcoin



Rules	Set by firm/org	Fixed by protocol
Infrastructure	Procured by firm/org	
Revenue	Fees set by firm/org	

Traditional Payment Systems vs. Bitcoin



Rules	Set by firm/org	Fixed by protocol
Infrastructure	Procured by firm/org	Revenue, entry/exit
Revenue	Fees set by firm/org	Equilibrium congestion pricing, all agents served

Related Literature

Blockchain

- Nakamoto (2008), Eyal & Sirer (2014), Sapirshtein et al. (2016), Narayan et al. (2016), Carlsten et al. (2016) Chiu & Koeppl (2017), Easley et al. (2017), Kroll et al. (2013)
- Usage of Bitcoin and the cryptocurrency market
 - Ron & Shamir (2013), Athey et al. (2016), Yermack (2013)
 - Gandal & Halaburda (2014), Halaburda & Sarvary (2016), Gans & Halaburda (2015), Catalini & Gans (2016), Cong & He (2017)

Queueing theory

 Lui (1985), Glazer & Hassin (1986), Hassin (1995), Hassin & Haviv (2003)

Talk outline

- Background the Blockchain protocol
 - "Blockchain for economists"
- Economic model of Bitcoin as a two-sided platform
 - Analytical solutions
 - Empirical evidence
- Implications and design considerations

The Blockchain ledger

- A bitcoin transaction is a balance transfer between addresses
- Sent publicly (to the mempool)



Coc80b7fb8fdd08cee477936df1f023a05df8e79f680b9b047e722c2e36534	8baa 🖪	mined Nor	/ 30, 2016 4:56:53 PM
15UAF2RS19XL6C7tJR8gsnys4z7PHTrLqd 19.4829 BTC	>	1NKGoZxNHupcfP7d1rzCyjaxDroiT4gdyw	3 BTC <mark>(S</mark>)
		1CkQwgCduA6YUhmG9ZhXaNjeERDoNdCSkk	16.4779 BTC (U)
FEE: 0.005 BTC		3 CONFIRMATIONS	19.4779 BTC

The Blockchain ledger

 A bitcoin transaction is a balance transfer between addresses



The Blockchain ledger is a list of all past transactions, organized into blocks



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- Many Miners, free entry
- All hold identical copies of the blockchain



New transactions transmitted to all miners

	Blockchain	
Miner 1		
Miner 2		
Miner 7		mempool

- Every 10 min (on avg), one randomly selected miner creates/mines a new block
- Maximal block size is 1MB (approx. 2000 transactions)
 - Unprocessed transactions remain, wait for next block



- New mined block transmitted to all miners
- Vetted by others, becomes part of the blockchain



Miners rewarded when mine a block:

- 1. Fixed amount of newly minted coins
 - Majority of current reward
 - Only short term, halved every 4 years
- 2. Transactions fees from transactions within the mined block
 - Long term
- Decentralized random selection by a tournament
 - Avoids the need for a trusted randomization device
 - Requires costly effort from each miner
 - Arrival of new blocks follows a Poisson process

- Equilibrium for (small) miners to follow the consensus blockchain (Nakamoto 2008, Eyal & Sirer 2013)
 - Only valid transactions verification using cryptography
 - Accept other's blocks follow the longest chain
 - With sufficiently many miners the system is secure

Blockchain – Properties

Users choose transaction fees

(Small) Miners are price takers

- Provide computational infrastructure, rewarded by transaction fees and newly minted coins
- Cannot block transactions, affect user behavior or transaction fees
- Free entry and exit of miners

System's throughput independent of number of miners

• Set by protocol parameters (1*MB*, 10min)

Simplified Economic Model

- N (small) miners
 - Equal computing power, equal cost of mining c_m
 - Many potential miners, free entry/exit
- Blocks mined at Poisson rate μ
 - Up to *K* transactions processed per block
- Users/transactions arrive at Poisson rate $\lambda < K \cdot \mu$
 - Each user has a single transaction, selects fee $b \ge 0$
 - Heterogeneous delay cost $c \sim F[0, \overline{c}]$

Simplified Economic Model

• Assumptions:

- Unobservable queue
- Sufficiently high value for service R, all users served
- No new coins minted
- Sufficiently many miners for the system to operate securely

Analysis of Miners

- In equilibrium, active miners maximize reward by procession K transactions with highest fees
 - Cannot affect the behavior of users or set transaction fees
 - Can observe pending transactions and their fees
 - Create block with highest fee transactions, up to block capacity

Analysis of Miners: Entry/Exit

- Total payment to miners is equal to total transaction fees
- Suppose *Rev* is total revenue (transaction fees) and there are *N* miners. Expected payment to each miner is

Free entry/exit imply zero profit, implying the number of miners is

$$N = \frac{Rev}{c_m}$$

Number of miners determined by Rev, c_m

Data: Cost per Transaction

	At max throughput 3.3 – 7 tx/sec	At real throughput 1.57 tx/sec	
Mining: hashing	~\$0.8 - \$1.7	~\$3.6	
Mining: hardware (~annual cost)	~\$0.6 - \$1.3	~\$2.7	
Transaction validation	~\$0.002	~\$0.008	
Bandwidth	~\$0.02	~\$0.08	
Storage (running cost)	~\$0.0008 / 5 years		

Source: Croman et.al (2016)

Data: Miners Costs and Revenue Oct 2015

Approx. total miners' cost (Croman et. al. 2016):

$$1.6 \frac{tx}{\sec} \cdot \frac{\$6}{tx} \cong \$10/\sec = \$6,000/10\min$$

Approx. \$325M annually

Approx. total reward:

25
$$\frac{btc}{10\text{min}} \cdot \frac{300}{btc} = \frac{7,500}{10\text{min}}$$

http://www.coinwarz.com/cryptocurrency



Analysis of Users/Transactions

- Users play a congestion queueing game
 - Blocks mined/added at rate µ, each processes K highest fee transactions
 - Transaction fees $b(c_i)$ are bids for priority
 - Independently of number of miners
- Equilibrium transaction fees $b_i = b(c_i)$ maximize

$$u(c_i) = \mathbf{R} - c_i \cdot W(b_i|G) - b_i$$

where $W(b_i|G)$ is the expected delay for a user who bids b_i given distribution of others bids G

Analysis of Users/Transactions

- Delay $W(b_i|G)$ depends only on
 - Arrival rate of higher priority transactions $\hat{\lambda}(b_i) = \lambda \cdot \overline{G}(b_i)$
 - Block size K, arrival rate μ
- In equilibrium $b(c_i)$ is increasing in c_i ,
 - $\bullet \ \bar{G}(b_i) = \bar{F}(c_i)$
- Solving for the stochastic behavior of the system

$$W\left(b \mid G\right) = \mu^{-1} W_{K}\left(\rho \cdot \bar{F}\left(c_{i}\right)\right)$$

- $\rho = \lambda / \mu K$ is a congestion parameter
- $\hat{\rho} = \hat{\lambda} / \mu K = \rho \, \overline{F}(c_i)$ is effective congestion for c_i

Expected Wait Formulas

Using generating functions, the expected wait of a transaction is

$$\mu^{-1} W_K(\hat{\rho}) = \frac{1}{\mu} \frac{1}{(1 - z_0) \left(1 + K\hat{\rho} + (K + 1) z_0^K\right)}$$

where

- $\hat{\rho} = \hat{\lambda}/K\mu$, where $\hat{\lambda}$ is the arrival rate of higher priority transactions
- z_0 is the solution in [0,1) of

$$z_0^{K+1} - (K\hat{\rho} + 1) \, z_0 + K\hat{\rho} = 0$$

Analysis of Users/Transactions

Lemma: In equilibrium,

- Users with higher delay costs pay higher transaction fees, receive higher priority and lower delay
- Transaction fee paid by a user is equal to the externality imposed on other transactions
 - $b(c_i) = \rho \int_0^{c_i} f(c) \cdot c \cdot \mu^{-1} W'_K \left(\rho \overline{F}(c)\right) dc$ $u(c_i) = R \int_0^{c_i} \mu^{-1} W_K \left(\rho \overline{F}(c)\right) dc$

Expected Delay for Lowest Priority Transaction given Congestion ρ

Delay (time)



Equilibrium Transaction Fees as Function of Congestion



Patameters: Ko=2,000, detay costs distributed c~U[0,1], $\mu = 1$

Equilibrium Transaction Fees as Function of User's Delay Cost



Patameters: K = 2,000, delay costs distributed $c \sim U[0,1]$, $\mu = 1$

User Payments

- Positive payments, without excluding transactions
 - Strictly positive net reward to all users
 - Even transaction that pay no fee are processed
- No monopoly pricing, even if the system is a monopoly to users
- But payments and delays vary with congestion
- In contrast, a monopolist would:
 - Process all transactions without delay
 - Set a minimal fee
 - Exclude some users, or eliminate consumer surplus

Equilibrium Revenue and Delay Costs

Theorem: In equilibrium, revenue (total fees), delay costs and number of miners depend only on the distribution of delay cost *F*, congestion $\rho = \lambda/K\mu$ and block size *K*.

$$DelayCosts = K\rho \int_{0}^{c} cf(c) \cdot W_{K}(\rho \bar{F}(c)) dc$$
$$Rev = K\rho^{2} \int_{0}^{\bar{c}} cf(c) \bar{F}(c) \cdot W_{K}'(\rho \bar{F}(c)) dc$$

and

$$N = Rev/c_m.$$

Equilibrium Revenue and Delay Costs 5000 -DelayCost delay cost, revenue (\$/time) 4000 Rev 3000 20001000 0 0.20.3 0.6 0.70.8 0.0 0.10.4 0.50.9

Congestion ρ

Parameters: K = 2,000, delay costs distributed $c \sim U[0,1]$

Equilibrium Fees and Delays

Corollary:

Equilibrium revenue (total fees), infrastructure level, and delay costs are increasing with congestion

$$Rev'(\rho) = K\rho \int_0^\infty \bar{W}'\left(\rho\bar{F}(c)\right)\bar{F}(c)^2 dc > 0$$
$$DC'(\rho) = (DC(\rho) + Rev(\rho))/\rho > 0$$

When $\rho = 0$ both Rev and DC are zero.

Data: Total Transaction Fees vs Congestion



Revenue and infrastructure

Infrastructure provided at cost

Free entry/exit, competition of miners

Revenue and infrastructure vary with congestion

- Revenue determines infrastructure level, but revenue does not depend on the need for infrastructure
- Infrastructure level can be too low or too high
- Congestion and delay costs are necessary for positive revenue

Potential Instability

Corollary: No Delays \Rightarrow No Revenues

- Low utilization ρ implies low revenue, miners exit
- Miners' exit does not generate congestion
 - System throughput is independent of number of miners
- System becomes unreliable with low number of miners (latency, vulnerability)
 - \blacktriangleright Potentially reducing user demand and ρ
 - Bad dynamics, leads to system collapse

Summary: Costs, Potential Waste

- Costly design
 - Redundancies, Tournament for random selection
- Delay costs are necessary to incentivize payment
- Infrastructure level (number of miners) may not be optimal
 - Determined by transaction fee payments due to congestion, not the need for more miners
- Costs can be smaller or larger than monopoly deadweight loss

Design: Controlling μ and K

- Instead of having a fixed capacity, we consider adjusting μ and *K* according to realized demand
 - Can be implemented in equilibrium, abstracting away from technological limits (such as network latency)
 - Need to understand the effect of bigger blocks versus more frequent blocks

Approximation for large K

Theorem:

As the block size K increases we have that

$$\lim_{K\to\infty}W_K(\widehat{\rho})=W_{\infty}(\widehat{\rho})$$

and

$$\operatorname{Rev}_{K}(\rho) = K \cdot \operatorname{Rev}_{\infty}(\rho) + o(K),$$
$$\operatorname{DelayCost}_{K}(\rho) = K \cdot \operatorname{DelayCost}_{\infty}(\rho) + o(K).$$

Convergence for Large K



Convergence for Large K



Revenue and Delay for Neglible Congestion

Theorem:

As $\rho \rightarrow 0$ we have that

$$\operatorname{Rev}_{\infty}(\rho) = O\left(e^{-1/\rho}\right),$$
$$\operatorname{DelayCost}_{\infty}(\rho) = \rho \cdot E\left[c\right] + o\left(\rho\right).$$

That is, delay costs are much larger than revenue for small ρ .

Controlling Congestion



Controlling Congestion



Summary

- Economic innovation of Blockchain technology
 - No owner
 - Competitive pricing, even if the platform is a monopoly
 - Fees determined in equilibrium
- Congestion as a revenue generating mechanism
 - System can raise revenue while serving all potential users
 - Requires congestion, delay costs
- Design of revenue generating rules
 - Control congestion to target revenue
 - Benefit of smaller block size
 - Future work what revenue generating rules are implementable?